

LECCION 3 - EJERCICIO 1 (14.1) v.2005 - SOLUTION TO GO FROM PLANE STRAIN TO PLANE STRESS

■ INICIO

```
Off [General::"spell1"]  
Off [General::"spell"]
```

```
ClearAll [Em, v, Emstar, vstar];
```

■ DEFINICION RELACION DEFORMACIONES-TENSIONES - DEFORMACION PLANA

□ FACTOR

E_m = MODULO ELASTICIDAD - ν = COEFICIENTE DE POISSON

? E

E is the exponential constant e (base of natural logarithms), with numerical value ≈ 2.71828 . >>

```
EfacDp = Em * (1 - v) / ((1 + v) * (1 - 2 v));
```

□ MATRIZ RELACION DEFORMACIONES-TENSIONES

```
Edp = EfacDp * {{1, v / (1 - v), 0}, {v / (1 - v), 1, 0}, {0, 0, (1 - 2 v) / (2 (1 - v))}};
```

```
Edp // MatrixForm
```

$$\begin{pmatrix} \frac{E_m (1-\nu)}{(1-2\nu)(1+\nu)} & \frac{E_m \nu}{(1-2\nu)(1+\nu)} & 0 \\ \frac{E_m \nu}{(1-2\nu)(1+\nu)} & \frac{E_m (1-\nu)}{(1-2\nu)(1+\nu)} & 0 \\ 0 & 0 & \frac{E_m}{2(1+\nu)} \end{pmatrix}$$

```
Edp / EfacDp // MatrixForm
```

$$\begin{pmatrix} 1 & \frac{\nu}{1-\nu} & 0 \\ \frac{\nu}{1-\nu} & 1 & 0 \\ 0 & 0 & \frac{1-2\nu}{2(1-\nu)} \end{pmatrix}$$

■ DEFINICION RELACION DEFORMACIONES-TENSIONES - TENSION PLANA

□ FACTOR

```
EfacTp = Em / (1 - v^2);
```

□ MATRIZ RELACION DEFORMACIONES-TENSIONES

$$Etp = EfacTp * \begin{pmatrix} 1 & \nu & 0 \\ \nu & 1 & 0 \\ 0 & 0 & \frac{1-\nu}{2} \end{pmatrix};$$

Etp // MatrixForm

$$\begin{pmatrix} \frac{Em}{1-\gamma^2} & \frac{Em \gamma}{1-\gamma^2} & 0 \\ \frac{Em \gamma}{1-\gamma^2} & \frac{Em}{1-\gamma^2} & 0 \\ 0 & 0 & \frac{Em(1-\gamma)}{2(1-\gamma^2)} \end{pmatrix}$$

Etp / EfacTp // MatrixForm

$$\begin{pmatrix} 1 & \gamma & 0 \\ \gamma & 1 & 0 \\ 0 & 0 & \frac{1-\gamma}{2} \end{pmatrix}$$

■ PLANTEAMIENTO DEL PROBLEMA

EdpS = Edp /. {Em → Emstar, γ → γstar};

EdpS // MatrixForm

$$\begin{pmatrix} \frac{Emstar(1-\gamma star)}{(1-2\gamma star)(1+\gamma star)} & \frac{Emstar \gamma star}{(1-2\gamma star)(1+\gamma star)} & 0 \\ \frac{Emstar \gamma star}{(1-2\gamma star)(1+\gamma star)} & \frac{Emstar(1-\gamma star)}{(1-2\gamma star)(1+\gamma star)} & 0 \\ 0 & 0 & \frac{Emstar}{2(1+\gamma star)} \end{pmatrix}$$

Etp // MatrixForm

$$\begin{pmatrix} \frac{Em}{1-\gamma^2} & \frac{Em \gamma}{1-\gamma^2} & 0 \\ \frac{Em \gamma}{1-\gamma^2} & \frac{Em}{1-\gamma^2} & 0 \\ 0 & 0 & \frac{Em(1-\gamma)}{2(1-\gamma^2)} \end{pmatrix}$$

□ IGUALAMOS DOS DE LOS TERMINOS - PORQUE DOS SON LAS INCOGNITAS: Emstar y γstar

EdpS[[1, 1]]

$$\frac{Emstar(1-\gamma star)}{(1-2\gamma star)(1+\gamma star)}$$

Etp[[1, 1]]

$$\frac{Em}{1-\gamma^2}$$

Ecuacion1 = EdpS[[1, 1]] == Etp[[1, 1]]

$$\frac{Emstar(1-\gamma star)}{(1-2\gamma star)(1+\gamma star)} == \frac{Em}{1-\gamma^2}$$

Ecuacion2 = EdpS[[1, 2]] == Etp[[1, 2]]

$$\frac{Emstar \gamma star}{(1-2\gamma star)(1+\gamma star)} == \frac{Em \gamma}{1-\gamma^2}$$

▣ RESOLVEMOS EL SISTEMA DE ECUACIONES

```
solucion = Solve[{Ecuacion1, Ecuacion2}, {Emstar, vstar}]
```

$$\left\{ \left\{ \text{Emstar} \rightarrow \frac{\text{Em} + 2 \text{Em} \nu}{(1 + \nu)^2}, \nu\text{star} \rightarrow \frac{\nu}{1 + \nu} \right\} \right\}$$

■ COMPROBACION

```
Simplify[EdpS /. solucion[[1]] // MatrixForm]
```

$$\begin{pmatrix} \frac{\text{Em}}{1-\nu^2} & \frac{\text{Em} \nu}{1-\nu^2} & 0 \\ \frac{\text{Em} \nu}{1-\nu^2} & \frac{\text{Em}}{1-\nu^2} & 0 \\ 0 & 0 & \frac{\text{Em}}{2+2\nu} \end{pmatrix}$$

```
Etp // MatrixForm
```

$$\begin{pmatrix} \frac{\text{Em}}{1-\nu^2} & \frac{\text{Em} \nu}{1-\nu^2} & 0 \\ \frac{\text{Em} \nu}{1-\nu^2} & \frac{\text{Em}}{1-\nu^2} & 0 \\ 0 & 0 & \frac{\text{Em} (1-\nu)}{2 (1-\nu^2)} \end{pmatrix}$$